

BENCHMARK COMPLEXITY REPORT

MATHEMATICS GRADE 8



Key: OCS Code = The benchmark code. Consists of Grade (K-8), Domain (2-3 character alpha code), Strand (1-3 character alpha code), Standard (1-9), Benchmark Number (1 or 1-1 and up), and Complexity (a, b, c).
Benchmark = The wording of the benchmark.
CCSS Code = Common Core State Standards, developed by National Governors Association Center for Best Practices, Council of Chief State School Officers (www.corestandards.org).
CRS Strand = ACT College Readiness Standards developed by ACT, Inc. (www.act.org).
The CRS Strands are: BOA = Basic Operations & Applications, PSD = Probability/Statistics/Data, NCP = Numbers/Concepts/Properties, XEI = Expression/Equation & Inequality, GRE = Graphical Representations, PPF = Properties of Plane Figures, MEA = Measurement, FUN = Functions.

| a. Low Complexity | | | | b. Intermediate Complexity | | | | c. High Complexity | | | |
|---|---|-----------|------------|----------------------------|---|-----------|------------|--------------------|---|-----------|------------|
| OCS Code | Benchmark | CCSS Code | CRS Strand | OCS Code | Benchmark | CCSS Code | CRS Strand | OCS Code | Benchmark | CCSS Code | CRS Strand |
| DOMAIN: Standards for Mathematical Content | | | | | | | | | | | |
| The Number System | | | | | | | | | | | |
| 8.SMC.NS.1.1-1.a | Show that numbers that are not rational are irrational | 8.NS.A.1 | NCP | 8.SMC.NS.1.2-1.b | Compare rational approximations of irrational numbers to the size of irrational numbers | 8.NS.A.2 | NCP | | | | |
| 8.SMC.NS.1.1-2.a | Show that every number has a decimal expansion | 8.NS.A.1 | NCP | 8.SMC.NS.1.2-2.b | Locate rational approximations of irrational numbers on a number line diagram | 8.NS.A.2 | GRE | | | | |
| 8.SMC.NS.1.1-3.a | Show that for rational numbers the decimal expansion repeats eventually | 8.NS.A.1 | NCP | 8.SMC.NS.1.2-3.b | Estimate the value of expressions by using rational approximations of irrational numbers | 8.NS.A.2 | NCP | | | | |
| 8.SMC.NS.1.1-4.a | Convert a decimal expansion which repeats eventually into a rational number | 8.NS.A.1 | NCP | | | | | | | | |
| Expressions and Equations | | | | | | | | | | | |
| 8.SMC.EE.1.1-1.a | Show that the properties of integer exponents generate equivalent numerical expressions | 8.EE.A.1 | NCP | 8.SMC.EE.1.2-1.b | Use square root symbols to represent solutions to equations of the form $x^2 = p$, where p is a positive rational number | 8.EE.A.2 | XEI | 8.SMC.EE.1.4-1.c | Perform operations with numbers expressed in scientific notation | 8.EE.A.4 | NCP |
| 8.SMC.EE.1.1-2.a | Apply the properties of integer exponents to generate equivalent numerical expressions | 8.EE.A.1 | NCP | 8.SMC.EE.1.2-2.b | Use cube root symbols to represent solutions to equations of the form $x^3 = p$, where p is a positive rational number | 8.EE.A.2 | XEI | 8.SMC.EE.1.4-2.c | Choose units of appropriate size for measurements of large or small quantities using scientific notation | 8.EE.A.4 | NCP |
| | | | | 8.SMC.EE.1.2-3.b | Evaluate square roots of small perfect squares | 8.EE.A.2 | NCP | 8.SMC.EE.1.4-3.c | Interpret numbers that have been expressed in scientific notation which have been generated by technology | 8.EE.A.4 | NCP |
| | | | | 8.SMC.EE.1.2-4.b | Evaluate cube roots of small perfect cubes | 8.EE.A.2 | NCP | 8.SMC.EE.3.3-4.c | Solve linear equations with rational number coefficients | 8.EE.C.7b | XEI |
| | | | | 8.SMC.EE.1.3-1.b | Estimate large or small quantities using numbers expressed in the form of a single digit times a whole-number power of 10 | 8.EE.A.3 | NCP | 8.SMC.EE.3.4-5.c | Solve real world and mathematical problems leading to two linear equations in two variables | 8.EE.C.8c | XEI |
| | | | | 8.SMC.EE.1.3-2.b | Compare large quantities to small quantities expressed in the form of a single digit times a whole-number power of 10 | 8.EE.A.3 | NCP | | | | |
| | | | | 8.SMC.EE.2.1-1.b | Graph proportional relationships | 8.EE.B.5 | GRE | | | | |
| | | | | 8.SMC.EE.2.1-2.b | Interpret the unit rate as the slope of a graph showing a proportional relationship | 8.EE.B.5 | GRE | | | | |
| | | | | 8.SMC.EE.2.1-3.b | Compare two different proportional relationships represented in different ways | 8.EE.B.5 | GRE | | | | |
| | | | | 8.SMC.EE.2.2-1.b | Use similar triangles to show that the slope m is the same between any two distinct points on a non-vertical line in the coordinate plane | 8.EE.B.6 | GRE | | | | |
| | | | | 8.SMC.EE.2.2-2.b | Derive the equation $y = mx$ for a line through the origin | 8.EE.B.6 | GRE | | | | |
| | | | | 8.SMC.EE.2.2-3.b | Derive the equation $y = mx + b$ for a line intercepting the vertical axis at b | 8.EE.B.6 | GRE | | | | |
| | | | | 8.SMC.EE.3.3-1.b | Create linear equations in one variable with one solution | 8.EE.C.7a | XEI | | | | |
| | | | | 8.SMC.EE.3.3-2.b | Create linear equations in one variable with infinitely many solutions | 8.EE.C.7a | XEI | | | | |
| | | | | 8.SMC.EE.3.3-3.b | Create linear equations in one variable with no solutions | 8.EE.C.7a | XEI | | | | |
| | | | | 8.SMC.EE.3.4-1.b | Show how solutions to a system of two linear equations in two variables correspond to points of intersection of their graph | 8.EE.C.8a | GRE | | | | |

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| | | | | 8.SMC.EE.3.4-2.b | Solve systems of two linear equations in two variables algebraically | 8.EE.C.8b | XEI | | | | |
| | | | | 8.SMC.EE.3.4-3.b | Estimate solutions of two linear equations by graphing the equations | 8.EE.C.8b | GRE | | | | |
| | | | | 8.SMC.EE.3.4-4.b | Solve simple cases of systems of two linear equations by inspection | 8.EE.C.8b | XEI | | | | |
| Functions | | | | | | | | | | | |
| 8.SMC.F.1.1-1.a | Recognize that a function is a rule that assigns to each input exactly one output | 8.F.A.1 | FUN | 8.SMC.F.1.2.b | Compare properties of two functions each represented in a different way | 8.F.A.2 | FUN | 8.SMC.F.1.3-1.c | Interpret the equation $y = mx + b$ as defining a linear function, whose graph is a straight line | 8.F.A.3 | GRE |
| 8.SMC.F.1.1-2.a | Relate the graph of a function to the set of ordered pairs consisting of an input and the corresponding output | 8.F.A.1 | GRE | 8.SMC.F.2.1-1.b | Construct a function to model a linear relationship between two quantities | 8.F.B.4 | GRE | 8.SMC.F.1.3-2.c | Construct examples of functions that are not linear | 8.F.A.3 | GRE |
| | | | | 8.SMC.F.2.1-2.b | Determine the rate of change and initial value of the function from a description of a relationship | 8.F.B.4 | GRE | 8.SMC.F.2.2-1.c | Describe qualitatively the functional relationship between two quantities by analyzing a graph | 8.F.B.5 | GRE |
| | | | | 8.SMC.F.2.1-3.b | Determine the rate of change and initial value of the function from two (x, y) values | 8.F.B.4 | GRE | 8.SMC.F.2.2-2.c | Graph the qualitative features of a function that has been described verbally | 8.F.B.5 | GRE |
| | | | | 8.SMC.F.2.1-4.b | Interpret the rate of change and initial value of a linear function in terms of the situation it models | 8.F.B.4 | GRE | | | | |
| | | | | 8.SMC.F.2.1-5.b | Interpret the rate of change and initial value of a linear function in terms of its graph | 8.F.B.4 | GRE | | | | |
| | | | | 8.SMC.F.2.1-6.b | Interpret the rate of change and initial value of a linear function in terms of a table of values | 8.F.B.4 | GRE | | | | |
| Geometry | | | | | | | | | | | |
| | | | | 8.SMC.G.1.1-1.b | Verify experimentally the properties of rotations, reflections, and translations, when lines are taken to lines | 8.G.A.1a | PPF | 8.SMC.G.1.5-1.c | State informal arguments to establish facts about the angle sum of triangles | 8.G.A.5 | PPF |
| | | | | 8.SMC.G.1.1-2.b | Verify experimentally the properties of rotations, reflections, and translations, when line segments are taken to line segments of the same length | 8.G.A.1a | PPF | 8.SMC.G.1.5-2.c | State informal arguments to establish facts about the exterior angle of triangles | 8.G.A.5 | PPF |
| | | | | 8.SMC.G.1.1-3.b | Verify experimentally the properties of rotations, reflections, and translations, when angles are taken to angles of the same measure | 8.G.A.1b | PPF | 8.SMC.G.1.5-3.c | State informal arguments to establish facts about the angles created when parallel lines are cut by a transversal | 8.G.A.5 | PPF |
| | | | | 8.SMC.G.1.1-4.b | Verify experimentally the properties of rotations, reflections, and translations, when parallel lines are taken to parallel lines | 8.G.A.1c | PPF | 8.SMC.G.1.5-4.c | State informal arguments to establish facts about the angle-angle criterion for similarity of triangles | 8.G.A.5 | PPF |
| | | | | 8.SMC.G.1.2-1.b | Show that a two-dimensional figure is congruent to another if the second can be obtained from the first by a sequence of rotations, reflections, and translations | 8.G.A.2 | MEA | 8.SMC.G.2.2-1.c | Solve real world and mathematical problems in two dimensions using the Pythagorean Theorem to determine unknown side lengths in right triangles | 8.G.B.7 | PPF |
| | | | | 8.SMC.G.1.2-2.b | Describe a sequence that exhibits the congruence between two congruent figures | 8.G.A.2 | MEA | 8.SMC.G.2.2-2.c | Solve real world and mathematical problems in three dimensions using the Pythagorean Theorem to determine unknown side lengths in right triangles | 8.G.B.7 | PPF |
| | | | | 8.SMC.G.1.3-1.b | Describe the effect of dilations on two-dimensional figures using coordinates | 8.G.A.3 | GRE | 8.SMC.G.2.3.c | Find the distance between two points in a coordinate system using the Pythagorean Theorem | 8.G.B.8 | PPF |
| | | | | 8.SMC.G.1.3-2.b | Describe the effect of translations on two-dimensional figures using coordinates | 8.G.A.3 | GRE | | | | |
| | | | | 8.SMC.G.1.3-3.b | Describe the effect of rotations on two-dimensional figures using coordinates | 8.G.A.3 | GRE | | | | |
| | | | | 8.SMC.G.1.3-4.b | Describe the effect of reflections on two-dimensional figures using coordinates | 8.G.A.3 | GRE | | | | |

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| | | | | 8.SMC.G.1.4-1.b | Relate one two-dimensional figure as similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and dilations | 8.G.A.4 | MEA | | | | |
| | | | | 8.SMC.G.1.4-2.b | Describe a sequence that exhibits the similarity between two similar two-dimensional figures | 8.G.A.4 | MEA | | | | |
| | | | | 8.SMC.G.2.1-1.b | Explain a proof of the Pythagorean Theorem | 8.G.B.6 | PPF | | | | |
| | | | | 8.SMC.G.2.1-2.b | Explain a proof of the converse of the Pythagorean Theorem | 8.G.B.6 | PPF | | | | |
| | | | | 8.SMC.G.3.1-1.b | Solve real world and mathematical problems using the formula for the volume of cones | 8.G.C.9 | MEA | | | | |
| | | | | 8.SMC.G.3.1-2.b | Solve real world and mathematical problems using the formula for the volume of cylinders | 8.G.C.9 | MEA | | | | |
| | | | | 8.SMC.G.3.1-3.b | Solve real world and mathematical problems using the formula for the volume of spheres | 8.G.C.9 | MEA | | | | |
| Statistics and Probability | | | | | | | | | | | |
| 8.SMC.SP.1.1-1.a | Construct scatter plots for bivariate measurement data | 8.SP.A.1 | PSD | 8.SMC.SP.1.2-1.b | Assess the proximity of data points to a line on a scatter plot in order to determine its linear association | 8.SP.A.2 | PSD | 8.SMC.SP.1.4-1.c | Analyze patterns of association of categorical data displayed in a two-way frequency and relative frequency table | 8.SP.A.4 | PSD |
| 8.SMC.SP.1.1-2.a | Analyze patterns of association between two quantities on a scatter plot of bivariate measurement data | 8.SP.A.1 | PSD | 8.SMC.SP.1.2-2.b | Assess the model fit to a line on a scatter plot by judging the closeness of the data points to a line | 8.SP.A.2 | PSD | 8.SMC.SP.1.4-2.c | Construct a two-way table summarizing data on two categorical variables collected from the same subjects | 8.SP.A.4 | PSD |
| | | | | 8.SMC.SP.1.3.b | Solve problems by interpreting the slope and intercept of bivariate measurement data by using the equation of a linear model | 8.SP.A.3 | PSD | 8.SMC.SP.1.4-3.c | Analyze summary data from a two-way frequency table to describe the association between two categorical variables | 8.SP.A.4 | PSD |
| DOMAIN: Standards for Mathematical Practices | | | | | | | | | | | |
| Solve Problems | | | | | | | | | | | |
| | | | | | | | | 8.SMP.1.c | Make sense of problems and persevere in solving them | MP1 | |
| Reason | | | | | | | | | | | |
| | | | | | | | | 8.SMP.2.c | Reason abstractly and quantitatively | MP2 | |
| Construct Arguments | | | | | | | | | | | |
| | | | | | | | | 8.SMP.3.c | Construct viable arguments and critique the reasoning of others | MP3 | |
| Model | | | | | | | | | | | |
| | | | | | | | | 8.SMP.4.c | Model with mathematics | MP4 | |
| Use Tools | | | | | | | | | | | |
| | | | | | | | | 8.SMP.5.c | Use appropriate tools strategically | MP5 | |
| Attend to Precision | | | | | | | | | | | |
| | | | | | | | | 8.SMP.6.c | Attend to precision | MP6 | |
| Use Structure | | | | | | | | | | | |
| | | | | | | | | 8.SMP.7.c | Look for and make use of structure | MP7 | |
| Express Regularity | | | | | | | | | | | |
| | | | | | | | | 8.SMP.8.c | Look for and express regularity in repeated reasoning | MP8 | |